

Midterm - Stat 4840/5084

Name _____

Thursday, March 6

Write directly on this exam. You may “show work” by handing in an R script, .Rmd file, or knit Markdown document.

You may use R, the internet, and any reference material. You are not allowed to communicate with anyone - no email, messaging, internet forums, AI, etc.

Honor Pledge

The work I have submitted represents my own effort. While working on this exam, I did not use generative AI or communicate in any form with individuals other than the instructor.

Signed:

Problem 1 (10 points)

Consider a random walk model $y_{t+1} = y_t + \epsilon_t$ where ϵ_t is white noise with variance 5. Suppose $y_0 = 8$.

a. What is $E[y_3]$?

b. What is $\text{Var}(y_3)$?

Problem 2 (10 points)

Consider a constant mean model $y_t = \mu + \epsilon_t$ where $\mu = 10$ and ϵ_t is white noise with variance 5.

a. What is $E[y_3]$?

b. What is $\text{Var}(y_3)$?

Problem 3 (10 points)

An electroencephalogram (EEG) is a record of electrical activity in the brain. The data `eeg.csv` is an EEG of a patient having a seizure, recorded at 256 values per second.

Load the data from our course data page and make an autocorrelogram with at least 300 lags.

What can you say about this EEG series by looking at its autocorrelation?

Problem 4 (10 points)

The `prices` data in the `fpp3` package has the annual price of copper (\$/lb) for most of the 20th century.

Filter the data to use only recent prices from the year 1920 onward.

Make a time plot of the series. Just looking at your plot (no need for precise answers):

a. When was copper cheapest and about how much did it cost per pound?

b. When was copper expensive and about how much did it cost per pound?

Problem 5 (10 points)

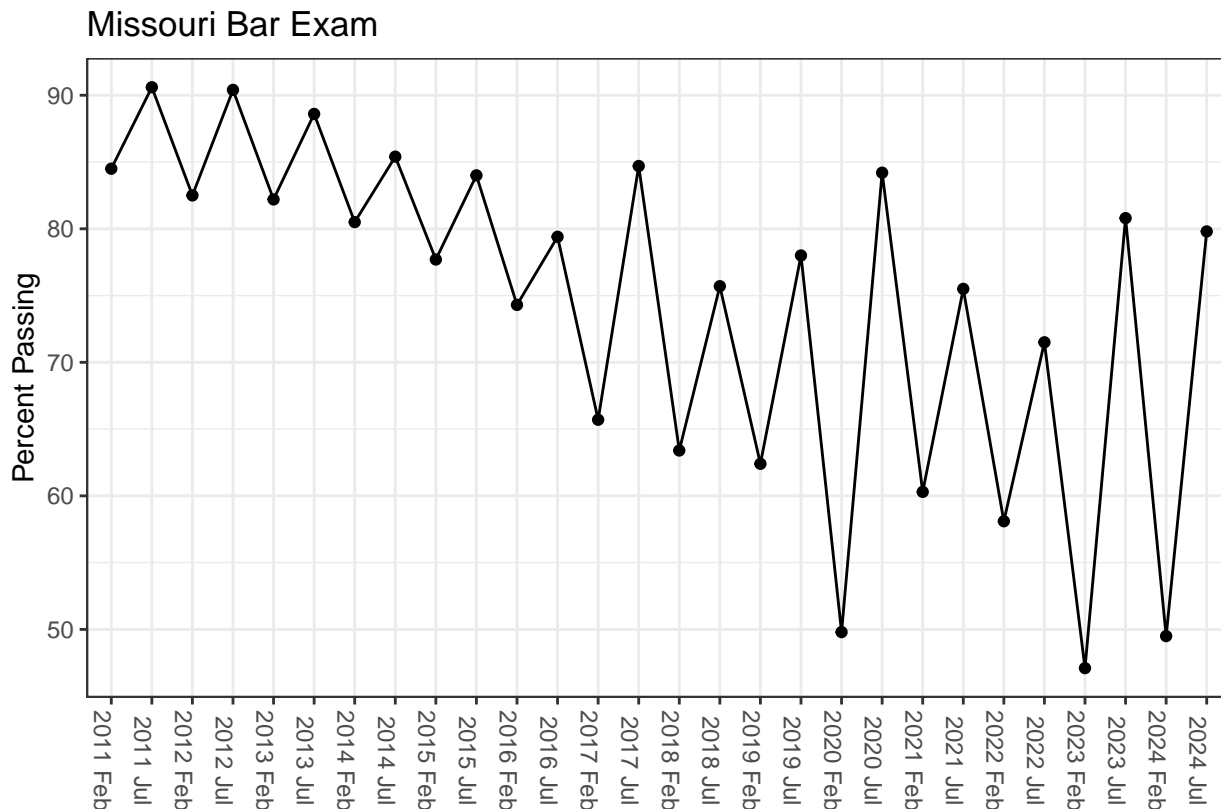
Continue with copper pricing from 1920-1997. Fit a naive/random walk model $y_{t+1} = y_t + \epsilon_t$ to the price series. The white noise term ϵ_t has variance σ^2 .

What is the model's estimate of σ^2 ?

Problem 9 (10 points)

To become a lawyer in the state of Missouri you need to pass the bar exam, which is offered every February and July.

The data `M0-bar-pass-rates.csv` on our course data page contains the percentage of people that passed the bar exam since 2011.



Make the `PctPass` into a base R time series with frequency 2, and perform a classical `decompose()` into trend, seasonal, and random components.

- Sketch the trend on the graph above.
- What is the seasonal difference between February and July pass rates?

Problem 10 (10 points)

- Find the 3-MA of the series $1, 1, -2, 1, 1, -2, 1, 1, -2, \dots$
- Give an example of a non-zero series with 5-MA equal to zero.