

A MacLaurin series is a Taylor series at  $x = 0$ :

$$C_0 + C_1x + C_2x^2 + C_3x^3 + \dots$$

where  $C_n = \frac{f^{(n)}(0)}{n!}$ .

1. Find the MacLaurin series for  $f(x) = e^x$  using the table below:

$n$	0	1	2	3	4	5
$f^{(n)}(x)$	$e^x$					
$f^{(n)}(0)$						
$C_n = \frac{f^{(n)}(0)}{n!}$						

Write the MacLaurin series for  $e^x$  using  $\dots$ , and also using summation notation ( $\Sigma$ ):

2. Use the 5th degree Taylor polynomial for  $e^x$  at  $x = 0$  to approximate  $e = e^1$ .
3. Find the MacLaurin series for  $g(x) = e^{x^2}$  by plugging in  $x^2$  to your previous series.
4. Find the 8<sup>th</sup> derivative of  $e^{x^2}$  at  $x = 0$ .