

Square Matrix Summary

\mathbf{A} is an $n \times n$ matrix.

Non-singular	Singular
\mathbf{A} has an inverse matrix	\mathbf{A} has no inverse matrix
$\mathbf{A}_R = \mathbf{I}$	\mathbf{A}_R has at least one row of zeros
rank $\mathbf{A} = n$ (full rank)	rank $\mathbf{A} < n$
image $\mathbf{A} = \mathbb{R}^n$	image \mathbf{A} is smaller than \mathbb{R}^n
nullity $\mathbf{A} = 0$	nullity $\mathbf{A} > 0$
kernel $\mathbf{A} = \{\mathbf{0}\}$	kernel \mathbf{A} is more than $\{\mathbf{0}\}$
$\mathbf{Ax} = \mathbf{0}$ has $\mathbf{x} = \mathbf{0}$ as its only solution	$\mathbf{Ax} = \mathbf{0}$ has nonzero solutions
$\mathbf{Ax} = \mathbf{b}$ has $\mathbf{x} = \mathbf{A}^{-1}\mathbf{b}$ as its only solution	$\mathbf{Ax} = \mathbf{b}$ has either no solutions or infinitely many solutions
The rows of \mathbf{A} form a basis for \mathbb{R}^n	The rows of \mathbf{A} are linearly dependent, and fail to span \mathbb{R}^n
The columns of \mathbf{A} form a basis for \mathbb{R}^n	The columns of \mathbf{A} are linearly dependent, and fail to span \mathbb{R}^n
$\det \mathbf{A} \neq 0$	$\det \mathbf{A} = 0$
All eigenvalues of \mathbf{A} are non-zero	0 is an eigenvalue of \mathbf{A}